## Members in Flexure \& Column Bases

$\therefore$ Total resistance provided by the pocket base
$=4.3[180 \times 480+n \times 20 \times 368]$ Newtons
Equating this to the external column load
$P=750 \mathrm{kN}=750 \times 10^{3}$ Newtons, we have
$750000=4.3[180 \times 480+n \times 20 \times 368]$, giving
$n=11.9$ say 12 members.
Provide 6 shear connectors on each side of the web of the column.
(see Figure 9.14)
Spacing of connectors $=5 d=5 \times 20=100 \mathrm{~mm}$
End cover $=200 \mathrm{~mm}$ of concrete below end plate.
Size of the pocket hole provided $200 \times 500 \mathrm{~mm} \times 1000 \mathrm{~mm}$ deep to be filled by mix M-15 cement concrete.

### 9.8 GRILLAGE FOUNDATION

When the foundation area required becomes too large, either due to heavy loads, or due to low bearing capacity of soil (or both), base slab type foundations become unsuitable.

One of the methods is to spread the column load to the foundation through a series of steel beams arranged at right angles to each other in two or more tiers.

Finally the beams are encased in lean concrete. Such foundations are called grillage foundations.

For a two tier grillage which is more common, the upper tier beams are connected to the column through a base plate. The lower tier beam which receives the load from the upper tier transfers it finally to the soil.

IS : 800 - has allowed an increase of $33 \frac{1}{3} \%$ over the usual permissible bending stresses in the case of grillage beams. If the loads include wind/earthquake or erection stresses an increase of $50 \%$ is allowed. Normally the following conditions have to be fulfilled.
a) Beams are to be unpainted and solidly encased in at least M-15 concrete with 10 mm aggregate,

(a)

b) Adjacent beam flanges are to be separated clear at least 75 mm apart by means of suitable separators,
c) Side and top concrete cones should be at least 100 mm all round the edges of beams/flanges.

The process of design will be clear by the following example.

## Example 9.9

Design a grillage foundation for a ISHB 400 column with a $300 \times 20 \mathrm{~mm}$ plate on each flanges.

Total load on the column is 2000 kN . The base plate is $650 \times 800 \mathrm{~mm}$. The bearing capacity of the soil is $120 \mathrm{kN} / \mathrm{m}^{2}$
(Permissible bending stress for beams is 165 MPa which may be increased by $33 \frac{1}{3} \%$ for the grillage beams.)

## Solution

Total load on column $\quad=2000 \mathrm{kN}$
Self weight of foundation (assumed $10 \%$ ) $=200 \mathrm{kN}$
Total load transmitted to soil $=2200 \mathrm{kN}$
Area of foundation required $=\frac{2200}{120}=18.33 \mathrm{~m}^{2}$
Assuming a $4.3 \times 4.3 \mathrm{~m}$ square foundation of area $=18.49 \mathrm{~m}^{2}$

Members in Flexure ", Column Bases

(a) Elevation

(b) Plan

Figure 9.16

## Top Tier Beams

Assuming 3 beams in the top-tier, which will be placed at right angles to the longer dimension ( 800 mm ) of the base plate.

Max. total B.M. $=\frac{W}{8}\left(l-l_{1}\right)=\frac{2000000}{8}(4300-650)=912,500,000$
Max. B.M. per beam $=\frac{912,500,000}{3}=304,167,000 \mathrm{Nmm}$
Permissible bending stress $=165 \times \frac{4}{3}=220 \mathrm{MPa}$
Required section modules $\mathrm{Z}=\frac{M}{f}=\frac{304,167,000}{220}=1383000 \mathrm{~mm}^{3}=1383 \mathrm{~cm}^{3}$
$\therefore \quad$ Adopt ISLB 500 nection ( $Z=1543.2 \mathrm{~cm}^{3}$ )
Max. total shear force for top tier beams $=\frac{W}{l}\left(\frac{l-l_{1}}{2}\right)$

$$
=\frac{2000,000}{4300}\left(\frac{4300-650}{2}\right)=848800 \mathrm{~N}
$$

S.F. per beam $=\frac{848800}{3}=282930 \mathrm{~N}$

Actual shear stress in beam web $=\frac{282930}{500 \times 9.2}$

$$
=61.5 \mathrm{MPa}<94.5 \mathrm{MPa} \text { permissible } \quad \therefore \text { OK. }
$$

Check for Vertical Web Buckling
Height of weg $(h)=500-2 \times 14.1=471.8 \mathrm{~mm}$
Web thickness $(t)=9.2 \mathrm{~mm}$
Slenderness ratio $=\frac{h}{t} \sqrt{3}=\frac{471.8}{9.2} \sqrt{3}=88.8$
Corresponding permissible compressive stress $=93.8 \mathrm{MPa}$
Length of spread for load $(B)=$ length of bearing plate $+\frac{1}{2}$ depth of beam

$$
=650+\frac{500}{2}=900 \mathrm{~mm}
$$

$\therefore \quad$ Corresponding bearing area for each beam $=$ B. $t=900 \times 9.2=8280 \mathrm{~mm}^{2}$
Total bearing area provided by three upper tier beams $=3 \times 8280=24840 \mathrm{~mm}^{2}$
$\therefore \quad$ Bearing stress $=\frac{2000000}{24840}=80.5 \mathrm{MPa}<93.8 \mathrm{MPa}$ (permissible)

## Check for Diagonal Buckling

For diagonal compression slenderness ratio $=\frac{h}{t} \sqrt{6}=\frac{471.8}{9.2} \sqrt{6}=125.6$
Corresponding allowable compressive stress $=63 \mathrm{MPa}>61.5 \mathrm{MPa}$ (actual shear stress) $\therefore \mathrm{OK}$.

## Design of Bottom Tier Beams

Using 10 Beams in the bottom tier. Maximum bending moment for the bottom tier beams $=\frac{W}{8}\left(l-l_{2}\right)$

$$
=\frac{2000000}{8}(4300-800)=875,000,000 \mathrm{Nmm}
$$

$\therefore \quad$ Maximum B.M. per beam $=\frac{875,000,000}{10}=87,500,000 \mathrm{Nmm}$
Permissible bending stress $=220 \mathrm{MPa}$
Section modulus required $=\frac{87,500,000}{220}=397727 \mathrm{~mm}^{3}=397.7 \mathrm{~cm}^{3}$
Provide ISMB 250 (section modulus $=410.5 \mathrm{~cm}^{3}$ )

Members in Flexure \& Column Bases

## Check for Shear

Maximum total shear force for bottom tier beam $=\frac{W}{l}\left(\frac{l-l_{2}}{2}\right)$

$$
=\frac{2,000,000}{4,300}\left(\frac{4300-800}{2}\right)=813900 \mathrm{~N}
$$

Shear force per mean $=\frac{813900}{10}=81390 \mathrm{~N}$
Shear stress $=\frac{\text { S.F. }}{\text { Web area }}=\frac{81390}{250 \times 6.9}=47.2 \mathrm{MPa}<94.5 \mathrm{MPa}$ (permissible)

## Check for Vertical Buckling

Slenderness ratio of web $=\frac{h}{t} \sqrt{3}=\left(\frac{250-2 \times 12.5}{6.9}\right) \sqrt{3}=56.5$
Corresponding permissible compressive stress $=114.5 \mathrm{MPa}$
Effective length for load spread $=$ length of bearing plate $+\frac{1}{2}$ depth of beam

$$
=800+\frac{250}{2}=925 \mathrm{~mm}
$$

Corresponding bearing area (each beam) $=925 \times 6.9=6383 \mathrm{~mm}^{2}$
Corresponding all ten webs $=63830 \mathrm{~mm}^{2}$
$\therefore \quad$ Bearing stress $=\frac{2,000,000}{63,830}=31.3 \mathrm{MPa}<$ Permissible stress $\therefore \mathrm{OK}$.

## Example 9.10 (Combined Grillage Foundation)

A combined grillage foundation is to be designed for two columns (A) \& (B) given the following data:

## Column Section Load

(A) $2 \times$ ISLC- 350 channels back to back (spacing 220 mm )
(B) $2 \times$ ISMC- 350 channels 1500 kN placed back to back (spacing 220 mm )
Spacing between the columns is 4.5 m centres.
Permissible stresses may be taken as follows:
bending (in steel beams) $\quad 220 \mathrm{MPa}$
direct compression (in steel beams) $\quad 252 \mathrm{MPa}$
shearing stress (in steel beams) 94.5 MPa
bearing (below base-plates) 4 MPa
safe bearing capacity of soil $150 \mathrm{kN} / \mathrm{m}^{2}$

## Solution

Load on column (A) ... 1000 kN
Load on column (B) ... 1500 kN

Total load
2750 kN
Safe bearing capacity (soil) $=150 \mathrm{kN} / \mathrm{m}^{2}$
$\therefore \quad$ Area of foundation required $=\frac{2750}{150}=18.33 \mathrm{~m}^{2}$


Figure 9.17
The plan of the foundation is so chosen that the C.G. of the foundation coincides with the C.G. of the loads. This is shown in Figure 9.17. If we assurne a minimum distance of 0.5 m to the left of the lighter-loaded column (A), the total length of the foundation comes as 6.4 m

$$
\therefore \quad \text { Width of foundation }=\frac{18.33}{6.4}=2.86 \mathrm{~m}(=2.9 \mathrm{~m} \mathrm{say})
$$

Area of base plate below column $(B)=\frac{1,500,000}{4}=375,000 \mathrm{~mm}^{2}$
Assuming a base plate of $600 \times 650 \mathrm{~mm}$ size and similar plate for column (A) also.

## Design of Top Tier Beams

The Top Tier Beams are parallel to the length of the foundation.
The sub-soil reaction per metre run $=\frac{1000+1500}{6.5}=390.6 \mathrm{kN} / \mathrm{m}$.
This can be assumed as an inverted overhanging beam supported at the column points (A) \& (B). The B.M. and S.F. diagrams are drawn in Figure 9.18, which must be verified by you.

Maximum B.M. for top tier $=780 \mathrm{kNm}$
Assuming three beams in the top tier.
B.M. per beam $=\frac{780}{3}=260 \mathrm{kNm}$

Section modulus ( z ) of each beam $=\frac{260,000,000}{220}=1,182,000 \mathrm{~mm}^{3}=1182 \mathrm{~cm}^{3}$
Choose ISMB 450 section ( $Z=1350.7 \mathrm{~cm}^{3}$ ).


## Check for Vertical Buckling under Column (B)

Column load on each beam $=\frac{1500}{3}=500 \mathrm{kN}$.
Effective spread length $(B)=$ Length of base plate + half the depth of beam

$$
=600+\frac{450}{2}=825 \mathrm{~mm}
$$

$$
\text { Buckling stress }=\frac{500,000}{825 \times 9.4}=64.5 \mathrm{MPa}
$$

[Flange thickness $\left(t_{f}\right)=17.4 \mathrm{~mm}$ \& web thickness $\left(t_{3}\right)=9.4 \mathrm{~mm}$ ]
$\therefore \quad$ Slenderness ratio of web $=\frac{h}{t} \sqrt{3}=\left(\frac{450-2 \times 17.4}{9.4}\right) \sqrt{3}=76.5$

Corresponding safe compressive stress $=103 \mathrm{MPa}>64.5 \mathrm{MPa}$ ( $\therefore$ Safe)

## Check for Shear

Maximum S.F. $=836.7 \mathrm{kN}$
S.F. per beam $=\frac{836.7}{3}=278.9 \mathrm{kN}$

Shear stress $=\frac{278,900}{450 \times 9.4}=65.9 \mathrm{MPa}<94.5 \mathrm{MPa}$ (permissible) $(\therefore$ safe $)$

## Check for Diagonal Buckling

Slenderness ratio $=\frac{h}{t} \sqrt{6} \frac{415.2}{9.4} \sqrt{6}=108.1$
Corresponding safe stress $=77 \mathrm{MPa}>65.9 \mathrm{MPa}$ (actual) $\therefore$ safe.
Design of Bottom Tier Beams
Maximum B.M. for bottom tier beam $=\frac{W}{8}\left(l-l_{2}\right)$

$$
=\frac{2,500,000}{8}[2900-650]=703100000 \mathrm{Nmm}
$$

Providing 12 beams in the lower tier
B.M. per beam $=\frac{703,100,000}{12}=58,592,000 \mathrm{Nmm}$

Section modulus : qquired per beam $(Z)=\frac{58,592,000}{200}=266400 \mathrm{~mm}^{3}=266.4 \mathrm{~cm}^{3}$
Use ISLB $250\left(Z=297.4 \mathrm{~cm}^{3}\right)$
Check for Vertical Buckling
Load per beam $\frac{2500000}{12}=208,300 \mathrm{~N}$
clear web height, $h=250-2 \times 8.2=233.6$; thickness $t=6.1$
slenderness ratio $=\frac{h}{t} \sqrt{3}=\frac{233.6}{6.1} \sqrt{3}=66.3$
corresponding safe compressive stress $=109.6 \mathrm{MPa}$
Effective length of beam for vertical buckling
$=$ Length of base plate + half the depth of beam
$=650+\frac{250}{2}=775 \mathrm{~mm}$
Buckling stress $=\frac{208300}{775 \times 601}=44.1 \mathrm{MPa}<109.6$ (permissible stress) $\therefore$ safe .
Check for Shear
Maximum S.F. for bottom tier $=\frac{W}{l}\left(\frac{l-l_{2}}{2}\right)=\frac{2,500,000}{2900}\left(\frac{2900-650}{2}\right)=969400 \mathrm{~N}$
S.F. per beam $=\frac{969400}{12}=8079 \mathrm{~N}$

Shear stress $=\frac{8079}{250 \times 6.1}=53 \mathrm{MPa}<94.5$ (permissible shear stress) $\quad \therefore \mathrm{OK}$.

Slenderness ratio for diagonal buckling $=\frac{h}{t} \sqrt{6}=\frac{233.6}{6.1} \sqrt{6}=94$
Corresponding safe compressive stress $=89.3 \mathrm{MPa}>53.0 \mathrm{MPa}$ (actual shear stress) $\therefore$ safe.

### 9.9 SUMMARY

All loads carried by columns are ultimately transferred to the Soil. As soil bearing pressures are much lower than steel strength, the relatively smaller column sections are to transfer the loads to a larger soil area. For this purpose suitable column bases and their connections are to be provided. The most common type is a slab base. For heavier loads gussetted bases are to be provided. Special arrangements are to be made for Moment resistant column bases. Grillage foundations are to be provided for very heavy column loads or poor bearing capacity soils, requiring a very large foundation area. The grillage beams which may be in several tiers are designed as (upward) loaded (cantilever) beams supported at the centre (column point).

### 9.10 ANSWERS TO SAQs

## SAQ 1

Refer Example 9.1

## SAQ 2

Refer Example 9.2

## SAQ 3

Refer Example 9.3

## FURTHER READING

## Design of Steel Structures by M. Raghupathi

Design of Steel Structures by Edwin H. Gaylord, Jr.Charies N. Gaylord
Design of Steel and Timber Structures by S.Ramanmrutham
Design of Steel Structures-Vol. I by Dr. Ramchandra
Design of Steel Structures by S.M.A. Kazmi\&R.S. Jindal
Design of Steel Structures by P. Dayarathnam
Design of Steel Structures by Prof. A.S. Arya \& J.L. Ajmani
Steel Structures and Timber Structures Analysis, Design and Details of Structures by V.N. Vazirani \& M.M. Ratwani

